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## Measurement of the fragmentation fraction ratio $f_s/f_d$ and its dependence on B meson kinematics

LHCb Collaboration ; et al ; Bernet, R ; Müller, K ; Steinkamp, O ; Straumann, U ; Vollhardt, A

**Abstract:** The relative production rate of  $B^0$ s and  $B^0$  mesons is determined with the hadronic decays  $B^0 \rightarrow D^- s^+$  and  $B^0 \rightarrow D^- K^+$ . The measurement uses data corresponding to  $1.0 \text{ fb}^{-1}$  of pp collisions at a centre-of-mass energy of  $\sqrt{s}=7 \text{ TeV}$  recorded in the forward region with the LHCb experiment. The ratio of production rates,  $f_s/f_d$ , is measured to be  $0.238 \pm 0.004 \pm 0.015 \pm 0.021$ , where the first uncertainty is statistical, the second systematic, and the third theoretical. This is combined with a previous LHCb measurement to obtain  $f_s/f_d = 0.256 \pm 0.020$ . The dependence of  $f_s/f_d$  on the transverse momentum and pseudorapidity of the B meson is determined using the decays  $B^0 \rightarrow D^- s^+$  and  $B^0 \rightarrow D^- K^+$ . There is evidence for a decrease with increasing transverse momentum, whereas the ratio remains constant as a function of pseudorapidity. In addition, the ratio of branching fractions of the decays  $B^0 \rightarrow D^- K^+$  and  $B^0 \rightarrow D^- s^+$  is measured to be  $0.0822 \pm 0.0011 \text{ (stat)} \pm 0.0025 \text{ (syst)}$ .

DOI: [https://doi.org/10.1007/JHEP04\(2013\)001](https://doi.org/10.1007/JHEP04(2013)001)

Posted at the Zurich Open Repository and Archive, University of Zurich

ZORA URL: <https://doi.org/10.5167/uzh-92008>

Journal Article

Published Version

Originally published at:

LHCb Collaboration; et al; Bernet, R; Müller, K; Steinkamp, O; Straumann, U; Vollhardt, A (2013). Measurement of the fragmentation fraction ratio  $f_s/f_d$  and its dependence on B meson kinematics. *Journal of High Energy Physics*, 2013:1.

DOI: [https://doi.org/10.1007/JHEP04\(2013\)001](https://doi.org/10.1007/JHEP04(2013)001)

# Measurement of the fragmentation fraction ratio $f_s/f_d$ and its dependence on $B$ meson kinematics



## The LHCb collaboration

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**ABSTRACT:** The relative production rate of  $B_s^0$  and  $B^0$  mesons is determined with the hadronic decays  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- K^+$ . The measurement uses data corresponding to  $1.0 \text{ fb}^{-1}$  of  $pp$  collisions at a centre-of-mass energy of  $\sqrt{s} = 7 \text{ TeV}$  recorded in the forward region with the LHCb experiment. The ratio of production rates,  $f_s/f_d$ , is measured to be  $0.238 \pm 0.004 \pm 0.015 \pm 0.021$ , where the first uncertainty is statistical, the second systematic, and the third theoretical. This is combined with a previous LHCb measurement to obtain  $f_s/f_d = 0.256 \pm 0.020$ . The dependence of  $f_s/f_d$  on the transverse momentum and pseudorapidity of the  $B$  meson is determined using the decays  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- \pi^+$ . There is evidence for a decrease with increasing transverse momentum, whereas the ratio remains constant as a function of pseudorapidity. In addition, the ratio of branching fractions of the decays  $B^0 \rightarrow D^- K^+$  and  $B^0 \rightarrow D^- \pi^+$  is measured to be  $0.0822 \pm 0.0011 \text{ (stat)} \pm 0.0025 \text{ (syst)}$ .

**KEYWORDS:** Hadron-Hadron Scattering, Branching fraction, B physics, Flavor physics

**ARXIV EPRINT:** [1301.5286](https://arxiv.org/abs/1301.5286)

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## Contents

|          |                                 |           |
|----------|---------------------------------|-----------|
| <b>1</b> | <b>Introduction</b>             | <b>1</b>  |
| <b>2</b> | <b>Detector and software</b>    | <b>2</b>  |
| <b>3</b> | <b>Event selection</b>          | <b>3</b>  |
| <b>4</b> | <b>Event yields</b>             | <b>4</b>  |
| <b>5</b> | <b>Systematic uncertainties</b> | <b>7</b>  |
| <b>6</b> | <b>Results</b>                  | <b>8</b>  |
| <b>7</b> | <b>Conclusions</b>              | <b>10</b> |
|          | <b>The LHCb collaboration</b>   | <b>13</b> |

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## 1 Introduction

The ratio of fragmentation fractions  $f_s/f_d$  quantifies the relative production rate of  $B_s^0$  mesons with respect to  $B^0$  mesons. Knowledge of this quantity is essential when determining any  $B_s^0$  branching fraction at the LHC. The measurement of the branching fraction of the rare decay  $B_s^0 \rightarrow \mu^+ \mu^-$  [1] is the prime example where a precise measurement of  $f_s/f_d$  is crucial for reaching the highest sensitivity in the search for physics beyond the Standard Model. The branching fractions of a large number of  $B^0$  and  $B^+$  decays have been measured to high precision at the  $B$  factories [2], but no  $B_s^0$  branching fraction is yet known with sufficiently high precision to be used as a normalisation channel.

The relative production rates of  $b$  hadrons are determined by the fragmentation fractions  $f_u, f_d, f_s, f_c$  and  $f_\Lambda$ , which describe the probability that a  $b$  quark will hadronize into a  $B_q$  meson (where  $q = u, d, s, c$ ), or a  $b$  baryon, respectively<sup>1</sup>. The ratio of fragmentation fractions  $f_s/f_d$  has been previously measured at LHCb with hadronic [3] and semileptonic decays [4], and the resulting values were combined [4].

In this paper, the ratio of fragmentation fractions  $f_s/f_d$  is determined using  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- K^+$  decays collected in  $pp$  collisions at a centre-of-mass energy of  $\sqrt{s} = 7 \text{ TeV}$ , with data corresponding to an integrated luminosity of  $1.0 \text{ fb}^{-1}$  recorded with the LHCb detector. Since the framework of factorization is well applicable to these decays [5], their ratio of branching fractions is theoretically well understood [6] and their

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<sup>1</sup>Charge conjugation is implied throughout this paper.

relative decay rates can be used to determine the ratio of fragmentation fractions for  $B_s^0$  and  $B^0$  mesons through

$$\begin{aligned} \frac{f_s}{f_d} &= \frac{\mathcal{B}(B^0 \rightarrow D^- K^+) \epsilon_{DK} N_{D_s \pi}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \pi^+) \epsilon_{D_s \pi} N_{DK}} \\ &= \Phi_{\text{PS}} \left| \frac{V_{us}}{V_{ud}} \right|^2 \left( \frac{f_K}{f_\pi} \right)^2 \frac{\tau_{B^0}}{\tau_{B_s^0}} \frac{1}{\mathcal{N}_a \mathcal{N}_F} \frac{\mathcal{B}(D^- \rightarrow K^+ \pi^- \pi^-) \epsilon_{DK} N_{D_s \pi}}{\mathcal{B}(D_s^- \rightarrow K^+ K^- \pi^-) \epsilon_{D_s \pi} N_{DK}}, \end{aligned} \quad (1.1)$$

where  $N$  corresponds to a signal yield,  $\epsilon$  corresponds to a total efficiency,  $\tau_{B_s^0}/\tau_{B^0} = 0.984 \pm 0.011$  [7] corresponds to the ratio of lifetimes and  $\mathcal{B}(D^- \rightarrow K^+ \pi^- \pi^-) = (9.14 \pm 0.20)\%$  [8] and  $\mathcal{B}(D_s^- \rightarrow K^+ K^- \pi^-) = (5.50 \pm 0.27)\%$  [9] correspond to the  $D_{(s)}^-$  meson branching fractions. The factor  $\mathcal{N}_a = 1.00 \pm 0.02$  accounts for the ratio of non-factorizable corrections [10],  $\mathcal{N}_F = 1.092 \pm 0.093$  for the ratio of  $B_{(s)}^0 \rightarrow D_{(s)}^-$  form factors [11], and  $\Phi_{\text{PS}} = 0.971$  for the difference in phase space due to the mass differences of the initial and final state particles. The numerical values used for the CKM matrix elements are  $|V_{us}| = 0.2252$ ,  $|V_{ud}| = 0.97425$ , and for the decay constants are  $f_\pi = 130.41$  MeV,  $f_K = 156.1$  MeV, with negligible uncertainties, below 1% [2]. The measurement is not statistically limited by the size of the  $B^0 \rightarrow D^- K^+$  sample, and therefore the theoretically less clean  $B^0 \rightarrow D^- \pi^+$  decays, where exchange diagrams contribute to the total amplitude, do not contribute to the knowledge of  $f_s/f_d$ .

The ratio of fragmentation fractions can depend on the centre-of-mass energy, as well as on the kinematics of the  $B_{(s)}^0$  meson, as was studied previously at LHCb with partially reconstructed  $B$  decays [4]. The dependence of the ratio of fragmentation fractions on the transverse momentum  $p_T$  and pseudorapidity  $\eta$  of the  $B_{(s)}^0$  meson is determined using fully reconstructed  $B^0 \rightarrow D^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  decays. Since it is only the dependence that is of interest here, the more abundant  $B^0 \rightarrow D^- \pi^+$  decay is used rather than the  $B^0 \rightarrow D^- K^+$  decay. The  $B^0 \rightarrow D^- K^+$  and  $B^0 \rightarrow D^- \pi^+$  decays are also used to determine their ratio of branching fractions, which can be used to quantify non-factorizable effects in such heavy-to-light decays [10].

The paper is organised as follows: the detector is described in section 2, followed by the event selection and the relative selection efficiencies in section 3. The fit to the mass distributions and the determination of the signal yields are discussed in section 4. The systematic uncertainties are presented in section 5, and the final results are given in section 6.

## 2 Detector and software

The LHCb detector [12] is a single-arm forward spectrometer covering the pseudorapidity range  $2 < \eta < 5$ , designed for the study of particles containing  $b$  or  $c$  quarks. The detector includes a high precision tracking system consisting of a silicon-strip vertex detector surrounding the  $pp$  interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes placed downstream. Data are taken with both magnet polarities. The combined tracking system has momentum resolution  $\Delta p/p$  that varies from

0.4% at 5 GeV/ $c$  to 0.6% at 100 GeV/ $c$ , and impact parameter<sup>2</sup> resolution of 20  $\mu\text{m}$  for tracks with high transverse momentum. Charged hadrons are identified using two ring-imaging Cherenkov detectors.

The trigger [13] consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage which applies a full event reconstruction. The events used in this analysis are selected at the hardware stage by requiring a cluster in the calorimeters with transverse energy larger than 3.6 GeV. The software stage requires a two-, three- or four-track secondary vertex with a high sum of the  $p_T$  of the tracks and a significant displacement from the primary  $pp$  interaction vertices (PVs). At least one track should have  $p_T$  greater than 1.7 GeV/ $c$ , track fit  $\chi^2$  over the number of degrees of freedom less than two, and IP  $\chi^2$  with respect to the associated primary interaction greater than sixteen. The IP  $\chi^2$  is defined as the difference between the  $\chi^2$  from the vertex fit of the associated PV reconstructed with and without the considered track. A multivariate algorithm is used for the identification of the secondary vertices consistent with the decay of a  $b$  hadron.

In the simulation,  $pp$  collisions are generated using PYTHIA 6.4 [14] with a specific LHCb configuration [15]. Decays of hadronic particles are described by EVTGEN [16], whilst final state radiation is generated using PHOTOS [17]. The interaction of the generated particles with the detector and its response are implemented using the GEANT4 toolkit [18, 19] as described in ref. [20].

### 3 Event selection

The three decay modes,  $B^0 \rightarrow D^-\pi^+$ ,  $B^0 \rightarrow D^-K^+$  and  $B_s^0 \rightarrow D_s^-\pi^+$ , are topologically very similar and can therefore be selected using the same event selection criteria, thus minimizing efficiency differences between the modes. The  $B_{(s)}^0$  candidates are reconstructed from a  $D_{(s)}^-$  candidate and an additional pion or kaon (the “bachelor” particle), with the  $D_{(s)}^-$  meson decaying to  $K^+\pi^-\pi^-$  ( $K^+K^-\pi^-$ ).

After the trigger selection, a loose preselection is made using the  $B_{(s)}^0$  and  $D_{(s)}^-$  masses, lifetimes and vertex qualities. A boosted decision tree (BDT) [21] is used to further separate signal from background. The BDT is trained on half the  $B_s^0 \rightarrow D_s^-\pi^+$  data sample. The most discriminating variables are the  $B_{(s)}^0$  impact parameter  $\chi^2$ , the pointing angle of the  $B_{(s)}^0$  candidate to the primary vertex and the  $p_T$  of the tracks. A cut value for the BDT output variable was chosen to optimally reduce the number of combinatorial background events, retaining approximately 84% of the signal events.

The  $D_{(s)}^-$  candidates are identified by requiring the invariant mass under the  $K^+\pi^-\pi^-$  ( $K^+K^-\pi^-$ ) hypothesis to fall within the selection window 1844–1890 (1944–1990) MeV/ $c^2$ . The relative efficiency of the selection procedure is evaluated for all decay modes using simulated events, generated with the appropriate Dalitz plot structures [22, 23]. Since the analysis is only sensitive to relative efficiencies, the impact of any discrepancy between data and simulation is small.

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<sup>2</sup>Impact parameter (IP) is defined as the transverse distance of closest approach between the track and a primary interaction.

The final  $B_s^0 \rightarrow D_s^- \pi^+$ ,  $B^0 \rightarrow D^- \pi^+$  and  $B^0 \rightarrow D^- K^+$  event samples are obtained after particle identification (PID) criteria, based on the difference in log-likelihood between the kaon and pion hypotheses (DLL). The PID performance as a function of  $p_T$  and  $\eta$  of the track is estimated from data using a calibration sample of approximately 27 million  $D^{*-} \rightarrow \bar{D}^0(K^+ \pi^-) \pi^-$  decays, which are selected using kinematic criteria only. A cut on the bachelor particle is placed at  $\text{DLL}(K - \pi) < 0$  to select the  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- \pi^+$  event samples and at  $\text{DLL}(K - \pi) > 5$  to select the  $B^0 \rightarrow D^- K^+$  sample. These requirements have an average efficiency of 85.5% and 73.0% respectively with a misidentification probability of 8.81% and 2.77%. The  $D_s^- \rightarrow K^+ K^- \pi^-$  decay is further distinguished from  $D^- \rightarrow K^+ \pi^- \pi^-$  decays by imposing  $\text{DLL}(K - \pi) > 5$  on the kaon candidate with the same charge as the  $D$  meson, whilst the DLL criteria for the  $\pi^-$  and  $K^+$  are identical between  $D^-$  and  $D_s^-$  and are used to discriminate  $D_{(s)}^-$  decays from background. The total (PID and invariant mass) efficiency to select the  $D^-$  ( $D_s^-$ ) particle is 84.6% (78.5%) with a misidentification probability of 4.57% (0.77%).

## 4 Event yields

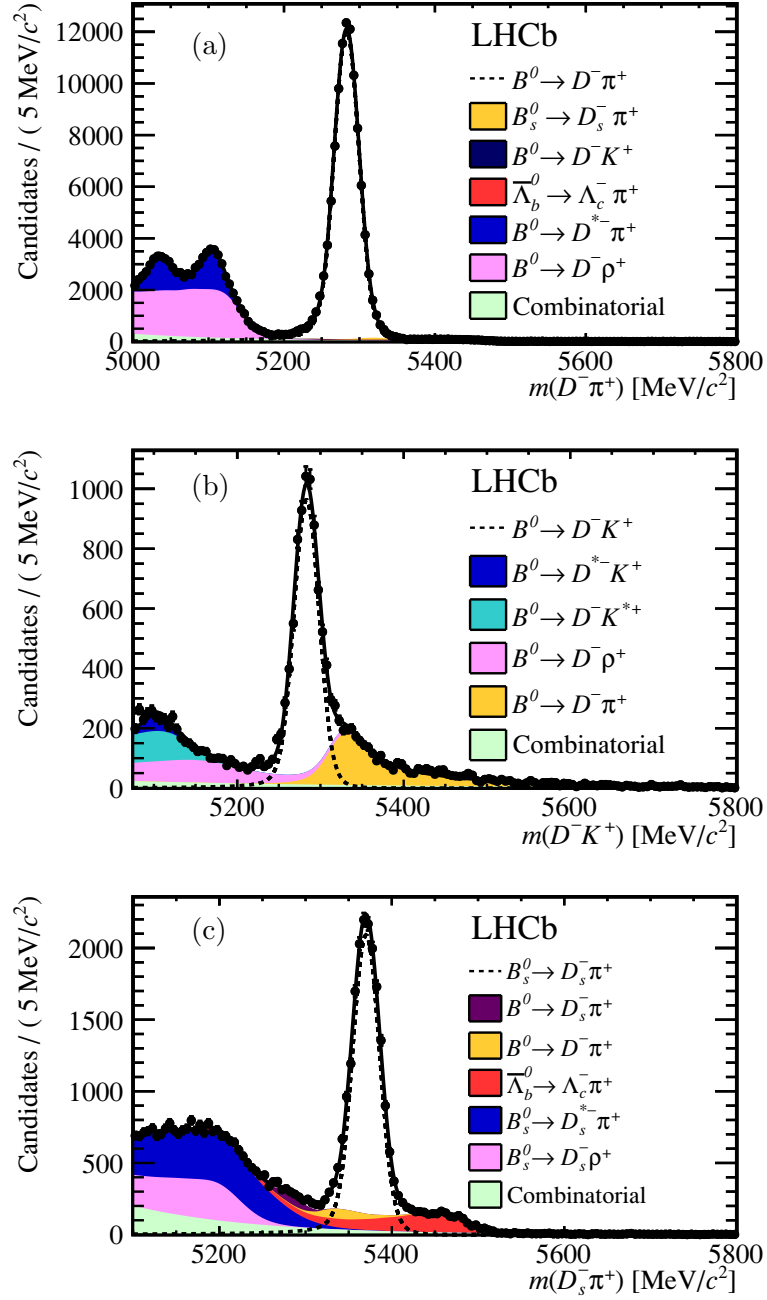
The relative yields of the three decay modes are determined from unbinned extended maximum likelihood fits to the mass distributions of the reconstructed  $B_{(s)}^0$  candidates as shown in figure 1. In order to achieve the highest sensitivity, the sample is separated according to the two magnet polarities, allowing for possible differences in PID performance and in running conditions. A simultaneous fit to the two magnet polarities is performed for each decay mode, with the peak position and width of each signal shared between the two.

The signal mass shape is described by a Gaussian distribution with power-law tails on either side to model the radiative tail and non-Gaussian detector effects. It consists of a Crystal Ball function [24]

$$f_{\text{left}}(m, \alpha, n, \mu, \sigma) = N \cdot \begin{cases} e^{-\frac{(m-\mu)^2}{2\sigma^2}}, & \text{for } \frac{m-\mu}{\sigma} > -\alpha \\ \left(\frac{n}{|\alpha|}\right)^n \cdot e^{-|\alpha|^2/2} \cdot \left(\frac{n}{|\alpha|} - |\alpha| - \frac{m-\mu}{\sigma}\right)^{-n}, & \text{for } \frac{m-\mu}{\sigma} \leq -\alpha \end{cases} \quad (4.1)$$

and a second, similar but mirrored, function to describe the right tail, resulting in the signal mass shape  $f_{\text{2CB}}(m) = f_{\text{left}}(m) + f_{\text{right}}(m)$ . The parameters of the tails are obtained from simulated events. The mean  $\mu$  and the width  $\sigma$  of the Gaussian distribution are equal in both Crystal Ball functions, and are allowed to vary in the fit. The parameter  $N$  is a normalisation factor.

Three classes of background are considered in the fit: fully reconstructed decays where at least one track is misidentified, partially reconstructed decays with or without misidentified tracks and combinatorial background. The shapes of the invariant mass distributions for the partially reconstructed decays are taken from large samples of simulated events. The main sources are  $B^0 \rightarrow D^- \rho^+$  and  $B^0 \rightarrow D^{*-} \pi^+(K^+)$  for the  $B^0 \rightarrow D^- \pi^+(K^+)$  sample, and  $B_s^0 \rightarrow D_s^- \rho^+$  and  $B_s^0 \rightarrow D_s^{*-} \pi^+$  for the  $B_s^0 \rightarrow D_s^- \pi^+$  sample.



**Figure 1.** Invariant mass distributions of (a)  $B^0 \rightarrow D^- \pi^+$  (b)  $B^0 \rightarrow D^- K^+$  and (c)  $B_s^0 \rightarrow D_s^- \pi^+$  candidates. The solid line is the result of the fit and the dotted line indicates the signal. The stacked background shapes follow the same top-to-bottom order in the legend and the plot. The  $B_s^0$  and  $\bar{\Lambda}_b^0$  backgrounds in the  $B^0 \rightarrow D^- \pi^+$  mass distribution are invisibly small. The resulting signal yields are listed in table 1. For illustration purposes the figures include events from both magnet polarities, although they are fitted separately as described in the text.

| Signal                          | Yield              |
|---------------------------------|--------------------|
| $B^0 \rightarrow D^- \pi^+$     | $106\,197 \pm 344$ |
| $B^0 \rightarrow D^- K^+$       | $7\,664 \pm 99$    |
| $B_s^0 \rightarrow D_s^- \pi^+$ | $17\,419 \pm 155$  |

**Table 1.** Yields obtained from the fits to the invariant mass distributions.

The invariant mass distributions of the misidentified decays are affected by the PID criteria. The shapes are obtained from simulated events, with the appropriate mass hypothesis applied. The distribution is then reweighted in a data-driven way, according to the particle identification cut efficiency obtained from the calibration sample, which is strongly dependent on the momentum of the particle.

Despite the small  $\pi \rightarrow K$  misidentification probability of 2.8%, the largest misidentified background in the  $B^0 \rightarrow D^- K^+$  sample originates from Cabibbo-favoured  $B^0 \rightarrow D^- \pi^+$  decays where the bachelor pion is misidentified as a kaon. The shape of this particular misidentified decay is determined from data using a high purity sample of  $B^0 \rightarrow D^- \pi^+$  decays (see figure 1(a)), obtained by selecting events in a narrow mass window 5200–5340 MeV/ $c^2$ . The yield of this prominent peaking background is allowed to vary in the fit and is found to be consistent with the expected yield based on the  $B^0 \rightarrow D^- \pi^+$  signal yield and the misidentification probability. The contamination of  $B^0 \rightarrow D^- \pi^+$  events in the  $B_s^0 \rightarrow D_s^- \pi^+$  sample can be caused by the misidentification of either pion from the  $D^-$  decay. The misidentification probability is 2.0% (3.2%) for the higher (lower)  $p_T$  pion. After selecting the  $D_s^-$  candidate within the mass window around the nominal  $D_s^-$  mass [2], the number of misidentified pions is reduced to 0.75% (0.02%). The yield of this background is constrained in the fit, based on the  $B^0 \rightarrow D^- \pi^+$  signal yield, the misidentification probability and their associated uncertainties.

The yield of  $\bar{A}_b^0 \rightarrow \Lambda_c^- \pi^+$  decays is allowed to vary in the fit. The cross-feeds from  $B^0 \rightarrow D^- K^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  events in the  $B^0 \rightarrow D^- \pi^+$  signal is small, and are constrained to their respective predicted yields. In addition, a contribution from the rare  $B^0 \rightarrow D_s^- \pi^+$  decay is expected with a yield of 3.3% compared to the  $B_s^0 \rightarrow D_s^- \pi^+$  signal, and is accounted for accordingly.

The combinatorial background consists of events with random pions and kaons, forming a fake  $D^-$  or  $D_s^-$  candidate, as well as real  $D^-$  or  $D_s^-$  mesons, that combine with a random pion or kaon. The combinatorial background is modelled with an exponential shape.

The results of the fits are presented in figure 1, and the corresponding signal yields are listed in table 1. The total yields of the decays  $B^0 \rightarrow D^- \pi^+$  and  $B^0 \rightarrow D^- K^+$  are used to determine the ratio of their branching fractions, while the event yields of the decays  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- K^+$  are used to measure the average ratio of fragmentation fractions.

The dependence of the relative  $b$ -hadron production fractions as a function of the transverse momentum and pseudorapidity of the  $B_{(s)}^0$  meson is studied in the ranges  $2.0 < \eta < 5.0$  and  $1.5 < p_T < 40$  GeV/ $c$ , using  $B^0 \rightarrow D^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  decays. The



| Source                      | $\frac{B^0 \rightarrow D^- \pi^+}{B^0 \rightarrow D^- K^+}$ (%) | $\frac{B_s^0 \rightarrow D_s^- \pi^+}{B^0 \rightarrow D^- K^+}$ (%) | $\frac{B_s^0 \rightarrow D_s^- \pi^+}{B^0 \rightarrow D^- \pi^+}$ (%) |
|-----------------------------|---|---|---|
| Detector acceptance         |   |   |   |
| and reconstruction          | 0.7   | 0.7   | 2.0 – 2.9   |
| Hardware trigger efficiency | 2.0   | 2.0   | 0.8   |
| Offline selection           | 1.2   | 1.1   | 1.2   |
| BDT cut                     | 1.0   | 1.0   | 1.5   |
| PID selection               | 1.0   | 1.5   | 1.1   |
| Comb. background            | 0.7   | 1.0   | 0.8   |
| Signal shape (tails)        | 0.5   | 0.6   | [correl.]   |
| Signal shape (core)         | 0.8   | 1.0   | [correl.]   |
| Charmless background        | 0.4   | —   | [correl.]   |
| Total                       | 3.1   | 3.4   | 3.2 – 3.8   |

**Table 2.** Systematic uncertainties for the measurement of the corrected ratio of event yields used for the measurements of  $f_s/f_d$  and the relative branching fraction of  $B^0 \rightarrow D^- K^+$ . The systematic uncertainty in  $p_T$  and  $\eta$  bins is shown as a range in the last column, and the total systematic uncertainty is the quadratic sum of the uncorrelated uncertainties. The systematic uncertainties on the ratio of  $B^0 \rightarrow D^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  yields that are correlated among the bins do not affect the dependence on  $p_T$  or  $\eta$ , and are not accounted for in the total systematic uncertainty.

event sample is subdivided in 20 bins in  $p_T$  and 10 bins in  $\eta$ , with the bin sizes chosen to obtain approximately equal number of events per bin. The fitting model for each bin is the same as that for the integrated samples, apart from the treatment of the exponent of the combinatorial background distribution, which is fixed to the value obtained from the fits to the integrated sample.

## 5 Systematic uncertainties

The systematic uncertainties on the measurement of the relative event yields of the  $B^0 \rightarrow D^- \pi^+$ ,  $B^0 \rightarrow D^- K^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  decay modes are related to trigger and offline selection efficiency corrections, particle identification calibration and the fit model.

The response to charged pions and kaons of the hadronic calorimeter used at the hardware trigger level has been investigated. As the hardware trigger mostly triggers on the high- $p_T$  bachelor, a systematic uncertainty of 2% is assigned to the ratio of trigger efficiencies for the decays  $B^0 \rightarrow D^- K^+$  and  $B^0 \rightarrow D^- \pi^+$ , estimated from dedicated studies with  $D^{*-} \rightarrow \bar{D}^0(K^+ \pi^-) \pi^-$  decays. This uncertainty is assumed to be uncorrelated between the individual bins in the binned analysis.

The relative selection efficiencies from simulation are studied by varying the BDT criterion, changing the signal yields by about  $\pm 25\%$ . The variation of the relative efficiency is 1.0% which is assigned as systematic uncertainty.

The uncertainty on the PID efficiencies is estimated by comparing, in simulated events, the results obtained using the  $D^{*-}$  calibration sample to the true simulated PID perfor-

mance on the signal decays. The corresponding uncertainty ranges from 1.0% to 1.5% for the different measurements.

The exponent of the combinatorial background distribution is allowed to vary in the fits to the  $B^0 \rightarrow D^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  mass distributions. By studying  $D^- \pi^-$  and  $D^- K^-$  combinations, it is suggested that the value of the exponent is smaller for the  $B^0 \rightarrow D^- K^+$  decays than for the  $B^0 \rightarrow D^- \pi^+$  decays, and therefore in the fit to the  $B^0 \rightarrow D^- K^+$  candidates the exponent is fixed to half the value found in the fit to the  $B^0 \rightarrow D^- \pi^+$  sample. The uncertainty on the signal yields due to the shape of the combinatorial background is estimated by reducing the exponent to half its value in the fits to the  $B^0 \rightarrow D^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  mass distributions, and by taking a flat background for the fit to the  $B^0 \rightarrow D^- K^+$  mass distribution. An uncertainty of 1.0% (0.7%) is assigned to the relative  $B^0 \rightarrow D^- K^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  ( $B^0 \rightarrow D^- \pi^+$ ) yields.

The tails of the signal distributions are fixed from simulation due to the presence of large amounts of partially reconstructed decays in the lower sidebands. The uncertainty on the signal yield is estimated by varying the parameters that describe the tails by 10%. The uncertainty from the shape of the central peak is taken from a fit allowing for two different widths for the Crystal Ball functions in eq. 4.1, leading to a 1.0% (0.8%) uncertainty on the relative  $B^0 \rightarrow D^- K^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  ( $B^0 \rightarrow D^- \pi^+$ ) yields.

The contribution of *charmless*  $B$  decays without an intermediate  $D$  meson is ignored in the fit. To evaluate the systematic uncertainty due to these decays, the  $B$  mass spectra for candidates in the sidebands of the  $D$  mass distribution are examined. A contribution of 0.4% relative to the signal yield is found in the  $B^0 \rightarrow D^- \pi^+$  decay mode, and no contribution is seen in the other modes. For the  $B^0 \rightarrow D^- \pi^+$  decay mode no correction is applied and the full size is taken as an uncertainty. No systematic uncertainty is assigned for the other decay modes.

The various sources of the systematic uncertainty that contribute to the uncertainties on the ratios of signal yields are listed in table 2. No uncertainty is associated to the  $\bar{A}_b^0 \rightarrow \Lambda_c^- \pi^+$  background, as the yield is allowed to vary in the fit. Other cross checks, like varying the  $B^0 \rightarrow D_s^- \pi^+$  yield in the  $B_s^0 \rightarrow D_s^- \pi^+$  fit or including  $\bar{A}_b^0 \rightarrow \Lambda_c^- K^+$  in the  $B^0 \rightarrow D^- K^+$  fit, show a negligible effect on the signal yields.

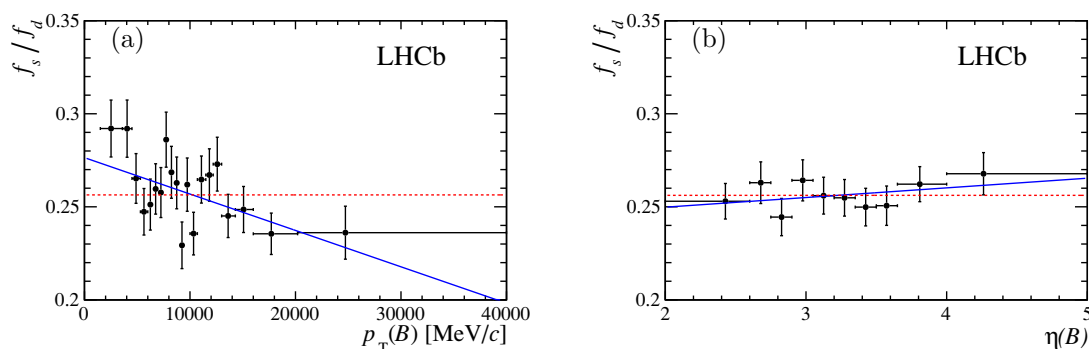
All systematic variations are also performed in bins, and the corresponding relative changes in the ratio of yields have been quantified. Variations showing correlated behaviour do not affect the slope and are therefore not considered further.

## 6 Results

The relative signal yields of the decays  $B^0 \rightarrow D^- \pi^+$ ,  $B^0 \rightarrow D^- K^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$  are used to determine the branching fraction of the decay  $B^0 \rightarrow D^- K^+$ , and the ratio of fragmentation fractions  $f_s/f_d$ .

The efficiency corrected ratio of  $B^0 \rightarrow D^- K^+$  and  $B^0 \rightarrow D^- \pi^+$  signal yields results in the ratio of branching fractions

$$\frac{\mathcal{B}(B^0 \rightarrow D^- K^+)}{\mathcal{B}(B^0 \rightarrow D^- \pi^+)} = 0.0822 \pm 0.0011 (\text{stat}) \pm 0.0025 (\text{syst}).$$



**Figure 2.** Ratio of fragmentation fractions  $f_s/f_d$  as functions of (a)  $p_T$  and (b)  $\eta$ . The errors on the data points are the statistical and uncorrelated systematic uncertainties added in quadrature. The solid line is the result of a linear fit, and the dashed line corresponds to the fit for the no-dependence hypothesis. The average value of  $p_T$  or  $\eta$  is determined for each bin and used as the center of the bin. The horizontal error bars indicate the bin size. Note that the scale is zero suppressed.

This is combined with the world average branching fraction  $\mathcal{B}(B^0 \rightarrow D^- \pi^+) = (26.8 \pm 1.3) \times 10^{-4}$  [2], to give

$$\mathcal{B}(B^0 \rightarrow D^- K^+) = (2.20 \pm 0.03 \pm 0.07 \pm 0.11) \times 10^{-4},$$

where the first uncertainty is statistical, the second is systematic and the last is due to the uncertainty on the  $B^0 \rightarrow D^- \pi^+$  branching fraction.

The ratio of fragmentation fractions is determined from the efficiency corrected event yields. The ratio of efficiencies is  $0.913 \pm 0.027$ . This results in

$$\begin{aligned} \frac{f_s}{f_d} &= (0.261 \pm 0.004 \pm 0.017) \times \frac{1}{\mathcal{N}_a \mathcal{N}_F} \\ &= 0.238 \pm 0.004 \pm 0.015 \pm 0.021, \end{aligned}$$

where the first uncertainty is statistical, the second is systematic containing the sources listed in table 2 as well as errors from external measurements, and the third is theoretical, due to the knowledge of  $\mathcal{N}_a$  and  $\mathcal{N}_F$ . The last source is dominated by the uncertainty on the form factor ratio.

This measurement supersedes and is in agreement with the previous determination with hadronic decays [3]. It also agrees with the previous measurement based on semileptonic decays [4]. The two independent results are combined taking into account the various sources of correlated systematic uncertainties, notably the  $D_{(s)}^-$  branching fractions and  $B_{(s)}^0$  lifetimes, to give

$$\frac{f_s}{f_d} = 0.256 \pm 0.020, \quad (6.1)$$

which supersedes the previous measurement from LHCb.

The value of  $f_s/f_d$  in bins of  $p_T$  or  $\eta$  is determined using the  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- \pi^+$  decay modes and is presented in figure 2. A linear  $\chi^2$  fit gives

$$\begin{aligned} f_s/f_d(p_T) &= (0.256 \pm 0.020) + (-2.0 \pm 0.6) \times 10^{-3} / \text{GeV}/c \times (p_T - \langle p_T \rangle) \\ f_s/f_d(\eta) &= (0.256 \pm 0.020) + (0.005 \pm 0.006) \times (\eta - \langle \eta \rangle), \end{aligned}$$

with  $\langle p_T \rangle = 10.4 \text{ GeV}/c$  and  $\langle \eta \rangle = 3.28$ . The data points are normalised with a scale factor to match the average value of 0.256. The uncertainty associated to this parameter is taken from eq. 6.1, whilst the error from the fit is 0.003 for both  $p_T$  and  $\eta$ .

The p-value for this linear fit is found to be 0.16 (0.87) for  $p_T$  ( $\eta$ ). The observed slope for the dependence on the transverse momentum of the  $B_{(s)}^0$  meson deviates from zero with a significance of three standard deviations. No indication of a dependence on  $\eta(B)$  is found.

## 7 Conclusions

The relative production rate of  $B_s^0$  and  $B^0$  mesons is determined using the hadronic decays  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- K^+$  resulting in  $f_s/f_d = 0.238 \pm 0.004(\text{stat}) \pm 0.015(\text{syst}) \pm 0.021(\text{theo})$ . This value is consistent with a previous LHCb measurement based on semileptonic decays, with which it is averaged to obtain  $f_s/f_d = 0.256 \pm 0.020$ . The ratio of fragmentation fractions  $f_s/f_d$  is determined as a function of the transverse momentum and pseudorapidity of the  $B_{(s)}^0$  meson, and a variation consistent with a linear dependence on the transverse momentum of the  $B_{(s)}^0$  meson is observed, with a significance of three standard deviations. In addition, the ratio of branching fractions of the decays  $B^0 \rightarrow D^- K^+$  and  $B^0 \rightarrow D^- \pi^+$  is measured to be  $0.0822 \pm 0.0011(\text{stat}) \pm 0.0025(\text{syst})$ .

## Acknowledgments

We express our gratitude to our colleagues in the CERN accelerator departments for the excellent performance of the LHC. We thank the technical and administrative staff at the LHCb institutes. We acknowledge support from CERN and from the national agencies: CAPES, CNPq, FAPERJ and FINEP (Brazil); NSFC (China); CNRS/IN2P3 and Region Auvergne (France); BMBF, DFG, HGF and MPG (Germany); SFI (Ireland); INFN (Italy); FOM and NWO (The Netherlands); SCSR (Poland); ANCS/IFA (Romania); MinES, Rosatom, RFBR and NRC “Kurchatov Institute” (Russia); MinECo, XuntaGal and GENCAT (Spain); SNSF and SER (Switzerland); NAS Ukraine (Ukraine); STFC (United Kingdom); NSF (USA). We also acknowledge the support received from the ERC under FP7. The Tier1 computing centres are supported by IN2P3 (France), KIT and BMBF (Germany), INFN (Italy), NWO and SURF (The Netherlands), PIC (Spain), GridPP (United Kingdom). We are thankful for the computing resources put at our disposal by Yandex LLC (Russia), as well as to the communities behind the multiple open source software packages that we depend on.

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